

銘傳大學九十學年度資訊管理研究所碩士班招生考試

財務金融
國際企業管理
經濟學
觀光

第二節

統計學 試題

請照題號順序作答，作答次序不符試卷所列，不予以評分。

可使用計算器。統計檢定題目一律用 0.05 顯著水準。答案小數點保留四位。

(一) 選擇題：十題(每題 4 分，共 40 分)

- (1) 一組樣本數為 10 所計算的平均數為 15。若事後發現其中一個樣本值從 7 修正為 17 時，其修正的平均數應為
(a) 15.33 (b) 15.7 (c) 16 (d) 17 (e) 以上皆非
- (2) 下列何者和變異數分析 (analysis of variance) 相關
(a) 檢定多個變異數是否相等 (b) 檢定多個平均數是否相等
(c) 檢定多個百分比是否相等 (d) 樣本數必須大於 30 (e) 以上皆非
- (3) 下列何者和列聯表 (contingency table) 分析並不相關
(a) 大樣本分析百分比 (b) 檢定獨立性
(c) 類別資料之分析 (d) 使用 χ^2 表 (e) 以上皆是
- (4) 波氏機率分配若其平均數為 6.4 時，則其標準差最接近之值為
(a) 12.8 (b) 3.2 (c) 2.53 (d) 6.4 (e) 以上皆非
- (5) 以雙尾檢定一個平均數時，若檢定統計 Z 值等於 2.08 時，其對應之 p 值為
(a) 0.0188 (b) 0.0376 (c) 0.0239 (d) 0.0478 (e) 0.0146
- (6) 下列何者為實驗設計中為達統計分析目的之基本原則
(a) 平均數相等變異數未知 (b) 平均數不相等變異數未知
(c) 平均數不相等變異數未知 (d) 隨機性、重複性、巨集性
(e) 母體為常態分配且變異數未知
- (7) 當以信賴區間估計一個母體的平均數時，該信賴區間的中心點值等於
(a) 樣本的平均數 (b) 母體的平均數
(c) 樣本的平均數加減估計誤差 (d) 樣本範圍除以 4 (e) 以上皆非

- (8) 以隨機樣本 400 個來估計一個母體的百分比時，其最大的標準誤 (standard error) 等於
 (a) 0.000625 (b) 0.025 (c) 0.049 (d) 0.062 (e) 以上皆非
- (9) 當以 t 檢定一個母體平均數時，劉母體的前題假設 (assumption) 為
 (a) 任何分配其變異數未知且抽樣個數多
 (b) 任何分配其變異數已知且抽樣個數少
 (c) 常態分配其變異數未知且抽樣個數少
 (d) 常態分配其變異數未知
 (e) 以上皆非
- (10) 在樣本數固定時檢定單個母體平均數，若希望降低結論錯誤之機率，下列敘述何者正確
 (a) 型一及型二誤差之機率可同時減少
 (b) 刪除樣本中之極端值可降低樣本變異
 (c) 固定型一誤差後，型二誤差之機率可減少
 (d) 確定母體為常態分配後，將虛無假設之設定值變小
 (e) 以上皆非

(二) 計算題：三題(共 60 分)

(1) A survey study is conducted on profit (in \$100,000) per house of speculative houses. The profit is derived mainly from the effect of two factors: house design (A, B, C) and area (east, west, south, and north) built. A random sample of size 3 is drawn for each factor level combination. The sample data are collected and the SAS output shows as follow, 20%

| SOURCE | DF | SUM of SQUARES | Mean SQUARE | F | PR>F |
|----------|----|----------------|-------------|------|--------|
| MODEL | 44 | 91.8697 | 8.3518 | 6.11 | 0.0001 |
| ERROR | 24 | 32.8200 | 1.3675 | | |
| C. TOTAL | 35 | 124.6897 | | | |

| SOURCE | DF | SUM of SQUARES | F VALUE | PR>F |
|-------------|----|----------------|---------|--------|
| DESIGN | 2 | 69.5417 | 8.48 | 0.0001 |
| AREA | 3 | 17.7275 | 4.32 | 0.0143 |
| DESIGN*AREA | 6 | 4.6006 | 1.68 | 0.2072 |

- (a) Write down the statistical model and the assumption for the analysis.
 Test the following hypothesis (state the 2 hypothesis, the p-value, and conclusion).
- (b) Do the data show sufficient evidence to indicate interaction between

factors of design and area?

(c) Do the data show sufficient evidence to indicate the effect of three designs is different?

(d) Do the data show sufficient evidence to indicate the effect of four areas is different?

(2) A manufacturer of automobile batteries claims that his product will last, on average, at least 4 years(i.e., 48 months). A consumer's advocate group wants to evaluate this longevity claim and selects a random sample of 26 such batteries to test. The data below indicate the length of time (in months) that each of these batteries lasted (i.e., performed properly before failure).

25.0, 30.7, 31.6, 34.1, 34.6, 37.2, 38.9, 39.2, 39.3, 39.6, 39.7, 40.8, 41.5,
42.3, 42.9, 44.1, 45.1, 47.0, 47.4, 49.0, 50.4, 51.8, 56.2, 57.3, 57.5, 60.1.

(The sample mean = 43.2039 and sample standard deviation = 8.8388)

The manufacturer has also stated in congressional testimony that the standard deviation in the life of the batteries produced is 9 months and, further, at least 90% of the batteries will last 3 years and can be called ‘reliable’. Test the following hypothesis (list the 2 hypothesis, the rejection region, test statistics, and conclusion). 25%

- (a) Find the sample median, minimum, maximum, and range.
 - (b) Is there evidence that significantly less than 90% of the batteries can be called ‘reliable’ ?
 - (c) Is there evidence that the average battery life is less than 48 months ?
 - (d) Is there evidence that the standard deviation in battery life exceeds 9 months ?
 - (e) What assumption must hold in order to perform the test in parts (c) and (d) ?

(3) Suppose that a weekly time series data of revenues (in billions) is recorded and the 3 week moving average and exponentially smoothing are partially listed below,

- (a) Fill in the blanks.

| Week | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|-----------------------------|-------|----|----|-------|-------|-------|-------|----|
| Revenue | 17 | 21 | 19 | 23 | 18 | 16 | 20 | 18 |
| Moving Average | | 19 | 21 | | | | | 18 |
| Exponentially Smoothing+ | 17.00 | | | 18.04 | 19.03 | 18.83 | 18.26 | |

*3 week moving
averages
+ smoothing constant,
 $\alpha=0.2$

(b) Compute the exponentially smoothing forecast for the 9th week.

TABLE 3 Normal Curve Areas

| <i>z</i> | .00 | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 0.0 | .0000 | .0040 | .0080 | .0120 | .0160 | .0199 | .0239 | .0279 | .0319 | .0359 |
| 0.1 | .0398 | .0438 | .0478 | .0517 | .0557 | .0596 | .0636 | .0675 | .0714 | .0753 |
| 0.2 | .0793 | .0832 | .0871 | .0910 | .0948 | .0987 | .1026 | .1064 | .1103 | .1141 |
| 0.3 | .1179 | .1217 | .1255 | .1293 | .1331 | .1368 | .1406 | .1443 | .1480 | .1517 |
| 0.4 | .1554 | .1591 | .1628 | .1664 | .1700 | .1736 | .1772 | .1808 | .1844 | .1879 |
| 0.5 | .1915 | .1950 | .1985 | .2019 | .2054 | .2088 | .2123 | .2157 | .2190 | .2224 |
| 0.6 | .2257 | .2291 | .2324 | .2357 | .2389 | .2422 | .2454 | .2486 | .2517 | .2549 |
| 0.7 | .2580 | .2611 | .2642 | .2673 | .2704 | .2734 | .2764 | .2794 | .2823 | .2852 |
| 0.8 | .2881 | .2910 | .2939 | .2967 | .2995 | .3023 | .3051 | .3078 | .3106 | .3133 |
| 0.9 | .3159 | .3186 | .3212 | .3238 | .3264 | .3289 | .3315 | .3340 | .3365 | .3389 |
| 1.0 | .3413 | .3438 | .3461 | .3485 | .3508 | .3531 | .3554 | .3577 | .3599 | .3621 |
| 1.1 | .3643 | .3665 | .3686 | .3708 | .3729 | .3749 | .3770 | .3790 | .3810 | .3830 |
| 1.2 | .3849 | .3869 | .3888 | .3907 | .3925 | .3944 | .3962 | .3980 | .3997 | .4015 |
| 1.3 | .4032 | .4049 | .4066 | .4082 | .4099 | .4115 | .4131 | .4147 | .4162 | .4177 |
| 1.4 | .4192 | .4207 | .4222 | .4236 | .4251 | .4265 | .4279 | .4292 | .4306 | .4319 |
| 1.5 | .4332 | .4345 | .4357 | .4370 | .4382 | .4394 | .4406 | .4418 | .4429 | .4441 |
| 1.6 | .4452 | .4463 | .4474 | .4484 | .4495 | .4505 | .4515 | .4525 | .4535 | .4545 |
| 1.7 | .4554 | .4564 | .4573 | .4582 | .4591 | .4599 | .4608 | .4616 | .4625 | .4633 |
| 1.8 | .4641 | .4649 | .4656 | .4664 | .4671 | .4678 | .4686 | .4693 | .4699 | .4706 |
| 1.9 | .4713 | .4719 | .4726 | .4732 | .4738 | .4744 | .4750 | .4756 | .4761 | .4767 |
| 2.0 | .4772 | .4778 | .4783 | .4788 | .4793 | .4798 | .4803 | .4808 | .4812 | .4817 |
| 2.1 | .4821 | .4826 | .4830 | .4834 | .4838 | .4842 | .4846 | .4850 | .4854 | .4857 |
| 2.2 | .4861 | .4864 | .4868 | .4871 | .4875 | .4878 | .4881 | .4884 | .4887 | .4890 |
| 2.3 | .4893 | .4896 | .4898 | .4901 | .4904 | .4906 | .4909 | .4911 | .4913 | .4916 |
| 2.4 | .4918 | .4920 | .4922 | .4925 | .4927 | .4929 | .4931 | .4932 | .4934 | .4936 |
| 2.5 | .4938 | .4940 | .4941 | .4943 | .4945 | .4946 | .4948 | .4949 | .4951 | .4952 |
| 2.6 | .4953 | .4955 | .4956 | .4957 | .4959 | .4960 | .4961 | .4962 | .4963 | .4964 |
| 2.7 | .4965 | .4966 | .4967 | .4968 | .4969 | .4970 | .4971 | .4972 | .4973 | .4974 |
| 2.8 | .4974 | .4975 | .4976 | .4977 | .4977 | .4978 | .4979 | .4979 | .4980 | .4981 |
| 2.9 | .4981 | .4982 | .4982 | .4983 | .4984 | .4984 | .4985 | .4985 | .4986 | .4986 |
| 3.0 | .4987 | .4987 | .4987 | .4988 | .4988 | .4989 | .4989 | .4990 | .4990 | .4990 |

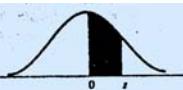


TABLE 4 Critical Values of *t*

| d.f. | <i>t</i> _{.050} | <i>t</i> _{.010} | <i>t</i> _{.005} | <i>t</i> _{.001} | <i>t</i> _{.0001} | d.f. |
|------|--------------------------|--------------------------|--------------------------|--------------------------|---------------------------|------|
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 | 1 |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 2 |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 3 |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 4 |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 5 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 6 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 7 |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 8 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 9 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 10 |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 11 |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 12 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 13 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 14 |
| 15 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 | 15 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 16 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 17 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 18 |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 19 |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 20 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 21 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 22 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 23 |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 24 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 25 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 26 |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 27 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 28 |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 29 |
| inf. | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 | inf. |

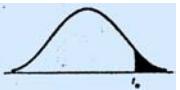
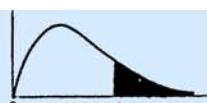


TABLE 5 Critical Values of Chi-square



| d.f. | $\chi^2_{0.99}$ | $\chi^2_{0.95}$ | $\chi^2_{0.90}$ | $\chi^2_{0.80}$ | $\chi^2_{0.70}$ | $\chi^2_{0.60}$ | $\chi^2_{0.50}$ | $\chi^2_{0.40}$ | $\chi^2_{0.30}$ | $\chi^2_{0.20}$ | $\chi^2_{0.10}$ | $\chi^2_{0.05}$ | $\chi^2_{0.01}$ | d.f. |
|------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|------|
| 1 | 0.0000393 | 0.0001571 | 0.0009821 | 0.0039321 | 0.0157908 | 0.20554 | 3.84146 | 5.02389 | 6.63490 | 7.87944 | 1 | | | |
| 2 | 0.0100251 | 0.0201007 | 0.0506356 | 0.102587 | 0.210720 | 4.60517 | 5.99147 | 7.37776 | 9.21034 | 10.5966 | 2 | | | |
| 3 | 0.0717212 | 0.114832 | 0.215795 | 0.351846 | 0.584375 | 6.25139 | 7.81473 | 9.34840 | 11.3449 | 12.8381 | 3 | | | |
| 4 | 0.206990 | 0.297110 | 0.484419 | 0.710721 | 1.063623 | 7.77944 | 9.48773 | 11.1433 | 13.2767 | 14.8602 | 4 | | | |
| 5 | 0.411740 | 0.554300 | 0.831211 | 1.145476 | 1.61031 | 9.23635 | 11.0705 | 12.8325 | 15.0863 | 16.7496 | 5 | | | |
| 6 | 0.675727 | 0.872085 | 1.237347 | 1.63539 | 2.0413 | 10.6446 | 12.5916 | 14.4494 | 16.8119 | 18.5476 | 6 | | | |
| 7 | 0.989265 | 1.239043 | 1.68987 | 2.16735 | 2.83311 | 12.0170 | 14.0671 | 16.0128 | 18.4753 | 20.2777 | 7 | | | |
| 8 | 1.344419 | 1.646482 | 2.17973 | 2.73264 | 3.48954 | 13.3616 | 15.5073 | 17.5346 | 20.0902 | 21.9550 | 8 | | | |
| 9 | 1.734926 | 2.087912 | 2.70039 | 3.32511 | 4.16816 | 14.6837 | 16.9190 | 19.0228 | 21.6660 | 23.5893 | 9 | | | |
| 10 | 2.15585 | 2.55821 | 3.24697 | 3.94030 | 4.86518 | 15.9871 | 18.3070 | 20.4831 | 23.2093 | 25.1882 | 10 | | | |
| 11 | 2.60321 | 3.05347 | 3.81575 | 4.57481 | 5.57779 | 17.2750 | 19.6751 | 21.9200 | 24.7250 | 26.7569 | 11 | | | |
| 12 | 3.07382 | 3.57056 | 4.40379 | 5.22603 | 6.30380 | 18.5494 | 21.0261 | 23.3367 | 26.2170 | 28.2995 | 12 | | | |
| 13 | 3.56503 | 4.10691 | 5.00874 | 5.89186 | 7.04150 | 19.8119 | 22.3621 | 24.7356 | 27.6883 | 29.8194 | 13 | | | |
| 14 | 4.07468 | 4.66043 | 5.62872 | 6.57063 | 7.78953 | 21.0642 | 23.6848 | 26.1190 | 29.1413 | 31.3193 | 14 | | | |
| 15 | 4.60094 | 5.22935 | 6.26214 | 7.26094 | 8.54675 | 22.3072 | 24.9958 | 27.4884 | 30.5779 | 32.8013 | 15 | | | |
| 16 | 5.14224 | 5.81221 | 6.90766 | 7.96164 | 9.31223 | 23.5418 | 26.2962 | 28.8454 | 31.9999 | 34.2672 | 16 | | | |
| 17 | 5.69724 | 6.40776 | 7.56418 | 8.67176 | 10.0852 | 24.7690 | 27.5871 | 30.1910 | 33.4087 | 35.7185 | 17 | | | |
| 18 | 6.26481 | 7.01491 | 8.23075 | 9.39046 | 10.8649 | 25.9894 | 28.8693 | 31.5264 | 34.8053 | 37.1564 | 18 | | | |
| 19 | 6.84398 | 7.63273 | 8.90655 | 10.1170 | 11.6509 | 27.2036 | 30.1435 | 32.8523 | 36.1908 | 38.5822 | 19 | | | |
| 20 | 7.43386 | 8.26040 | 9.59083 | 10.8508 | 12.4426 | 28.4120 | 31.4104 | 34.1696 | 37.5662 | 39.9968 | 20 | | | |
| 21 | 8.03366 | 8.89720 | 10.28293 | 11.5913 | 13.2396 | 29.6151 | 32.6705 | 35.4789 | 38.9321 | 41.4010 | 21 | | | |
| 22 | 8.64272 | 9.54249 | 10.9823 | 12.3380 | 14.0415 | 30.8133 | 33.9244 | 36.7807 | 40.2894 | 42.7956 | 22 | | | |
| 23 | 9.26042 | 10.19567 | 11.6885 | 13.0905 | 14.8479 | 32.0069 | 35.1725 | 38.0757 | 41.6384 | 44.1813 | 23 | | | |
| 24 | 9.88623 | 10.8564 | 12.4011 | 13.8484 | 15.6587 | 33.1963 | 36.4151 | 39.3641 | 42.9798 | 45.5585 | 24 | | | |
| 25 | 10.5197 | 11.5240 | 13.1197 | 14.6114 | 16.4734 | 34.3816 | 37.6525 | 40.6465 | 44.3141 | 49.9278 | 25 | | | |
| 26 | 11.1603 | 12.1981 | 13.8439 | 15.3791 | 17.2919 | 35.5631 | 38.8852 | 41.9232 | 45.6417 | 48.2899 | 26 | | | |
| 27 | 11.8076 | 12.8786 | 14.5733 | 16.1513 | 18.1138 | 36.7412 | 40.1133 | 43.1944 | 46.9630 | 49.6449 | 27 | | | |
| 28 | 12.4613 | 13.5648 | 15.3079 | 16.9279 | 18.9392 | 37.9159 | 41.3372 | 44.4607 | 48.2782 | 50.9933 | 28 | | | |
| 29 | 13.1211 | 14.2565 | 16.0471 | 17.7083 | 19.7677 | 39.0875 | 42.5569 | 45.7222 | 49.5879 | 52.3356 | 29 | | | |
| 30 | 13.7867 | 14.9535 | 16.7908 | 18.4926 | 20.5992 | 40.2560 | 43.7729 | 46.9792 | 50.8922 | 53.6720 | 30 | | | |
| 40 | 20.7065 | 22.1643 | 24.4331 | 26.5093 | 29.0505 | 51.8050 | 55.7585 | 59.3417 | 63.6907 | 66.7659 | 40 | | | |
| 50 | 27.9907 | 29.7067 | 32.3574 | 34.7642 | 37.6886 | 63.1671 | 67.5048 | 71.4202 | 76.1539 | 79.4900 | 50 | | | |
| 60 | 35.5346 | 37.4848 | 40.4817 | 43.1879 | 46.4589 | 74.3970 | 79.0819 | 83.2976 | 88.3794 | 91.9317 | 60 | | | |
| 70 | 43.2752 | 45.4418 | 48.7576 | 51.7393 | 55.3290 | 85.5271 | 90.5312 | 95.0231 | 100.425 | 104.215 | 70 | | | |
| 80 | 51.1720 | 53.5400 | 57.1532 | 60.3915 | 64.2778 | 96.5782 | 101.879 | 106.629 | 112.329 | 116.321 | 80 | | | |
| 90 | 59.1963 | 61.7541 | 65.6466 | 69.1260 | 73.2912 | 107.565 | 113.145 | 118.116 | 124.116 | 128.299 | 90 | | | |
| 100 | 67.3276 | 70.0648 | 74.2219 | 77.9295 | 82.3581 | 118.498 | 124.342 | 129.561 | 135.807 | 140.169 | 100 | | | |

TABLE 6 Percentage Points of the F Distribution: $\alpha = .05$ 

| v_1 (d.f.) | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 12 | 15 | 20 | 24 | 30 | 40 | 60 | 120 | v_2 (d.f.) |
|--------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-------|-------|-------|-------|-------|-------|-------|--------------|
| 1 | 161.4 | 199.5 | 215.7 | 224.6 | 230.2 | 234.0 | 236.8 | 238.9 | 240.5 | 241.9 | 243.9 | 245.9 | 248.0 | 249.1 | 250.1 | 251.1 | 252.2 | 253.3 | 254.3 |
| 2 | 18.51 | 19.00 | 19.16 | 19.25 | 19.30 | 19.33 | 19.35 | 19.37 | 19.38 | 19.40 | 19.41 | 19.43 | 19.45 | 19.45 | 19.46 | 19.47 | 19.48 | 19.49 | 19.50 |
| 3 | 10.13 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.89 | 8.85 | 8.81 | 8.79 | 8.74 | 8.70 | 8.66 | 8.64 | 8.62 | 8.59 | 8.57 | 8.55 | 8.53 |
| 4 | 7.71 | 6.94 | 6.59 | 6.39 | 6.26 | 6.16 | 6.09 | 6.04 | 6.00 | 5.96 | 5.91 | 5.86 | 5.80 | 5.77 | 5.75 | 5.72 | 5.69 | 5.66 | 5.63 |
| 5 | 6.61 | 5.79 | 5.41 | 5.19 | 5.05 | 4.95 | 4.88 | 4.82 | 4.77 | 4.74 | 4.68 | 4.62 | 4.56 | 4.53 | 4.50 | 4.46 | 4.43 | 4.40 | 4.36 |
| 6 | 5.99 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.21 | 4.15 | 4.10 | 4.06 | 4.00 | 3.94 | 3.87 | 3.84 | 3.81 | 3.77 | 3.74 | 3.70 | 3.67 |
| 7 | 5.59 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.79 | 3.73 | 3.68 | 3.64 | 3.57 | 3.51 | 3.44 | 3.41 | 3.38 | 3.34 | 3.30 | 3.27 | 3.23 |
| 8 | 5.32 | 4.46 | 4.07 | 3.84 | 3.69 | 3.58 | 3.50 | 3.44 | 3.39 | 3.35 | 3.28 | 3.22 | 3.15 | 3.12 | 3.08 | 3.04 | 3.01 | 2.97 | 2.93 |
| 9 | 5.12 | 4.26 | 3.86 | 3.63 | 3.48 | 3.37 | 3.29 | 3.23 | 3.18 | 3.14 | 3.07 | 3.01 | 2.94 | 2.90 | 2.86 | 2.83 | 2.79 | 2.75 | 2.71 |
| 10 | 4.96 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.14 | 3.07 | 3.02 | 2.98 | 2.91 | 2.85 | 2.77 | 2.74 | 2.70 | 2.66 | 2.62 | 2.58 | 2.54 |
| 11 | 4.84 | 3.98 | 3.59 | 3.36 | 3.20 | 3.09 | 3.01 | 2.95 | 2.90 | 2.85 | 2.79 | 2.72 | 2.65 | 2.61 | 2.57 | 2.53 | 2.49 | 2.45 | 2.40 |
| 12 | 4.75 | 3.89 | 3.49 | 3.26 | 3.11 | 3.00 | 2.91 | 2.85 | 2.80 | 2.75 | 2.69 | 2.62 | 2.54 | 2.51 | 2.47 | 2.43 | 2.38 | 2.34 | 2.30 |
| 13 | 4.67 | 3.81 | 3.41 | 3.18 | 3.03 | 2.92 | 2.83 | 2.77 | 2.71 | 2.67 | 2.60 | 2.53 | 2.46 | 2.42 | 2.38 | 2.34 | 2.30 | 2.25 | 2.21 |
| 14 | 4.60 | 3.74 | 3.34 | 3.11 | 2.96 | 2.85 | 2.76 | 2.70 | 2.65 | 2.60 | 2.53 | 2.46 | 2.39 | 2.35 | 2.31 | 2.27 | 2.22 | 2.18 | 2.13 |
| 15 | 4.54 | 3.68 | 3.29 | 3.06 | 2.90 | 2.71 | 2.64 | 2.59 | 2.54 | 2.48 | 2.40 | 2.33 | 2.29 | 2.25 | 2.20 | 2.16 | 2.11 | 2.07 | 2.05 |
| 16 | 4.49 | 3.63 | 3.24 | 3.01 | 2.85 | 2.74 | 2.66 | 2.59 | 2.54 | 2.49 | 2.42 | 2.35 | 2.28 | 2.24 | 2.19 | 2.15 | 2.11 | 2.06 | 2.01 |
| 17 | 4.45 | 3.59 | 3.20 | 2.96 | 2.81 | 2.70 | 2.61 | 2.55 | 2.49 | 2.45 | 2.38 | 2.31 | 2.23 | 2.19 | 2.15 | 2.10 | 2.06 | 2.01 | 1.96 |
| 18 | 4.41 | 3.55 | 3.16 | 2.93 | 2.77 | 2.66 | 2.58 | 2.51 | 2.46 | 2.41 | 2.34 | 2.27 | 2.19 | 2.15 | 2.11 | 2.06 | 2.02 | 1.97 | 1.92 |
| 19 | 4.38 | 3.52 | 3.13 | 2.90 | 2.74 | 2.63 | 2.54 | 2.48 | 2.42 | 2.38 | 2.31 | 2.23 | 2.16 | 2.11 | 2.07 | 2.03 | 1.98 | 1.93 | 1.88 |
| 20 | 4.35 | 3.49 | 3.10 | 2.87 | 2.71 | 2.60 | 2.51 | 2.45 | 2.39 | 2.35 | 2.28 | 2.20 | 2.12 | 2.08 | 2.04 | 1.99 | 1.95 | 1.90 | 1.84 |
| 21 | 4.32 | 3.47 | 3.07 | 2.84 | 2.68 | 2.57 | 2.49 | 2.42 | 2.37 | 2.32 | 2.25 | 2.18 | 2.10 | 2.05 | 2.01 | 1.96 | 1.92 | 1.87 | 1.81 |
| 22 | 4.30 | 3.44 | 3.05 | 2.82 | 2.66 | 2.55 | 2.46 | 2.40 | 2.34 | 2.30 | 2.23 | 2.15 | 2.07 | 2.03 | 1.98 | 1.94 | 1.89 | 1.84 | 1.78 |
| 23 | 4.28 | 3.42 | 3.03 | 2.80 | 2.64 | 2.53 | 2.44 | 2.37 | 2.32 | 2.27 | 2.20</ | | | | | | | | |

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